MAY 2006 AMERICAN MATHEMATICAL MONTHLY PROBLEM

11123. Proposed by Christopher Hillar, Texas A& M University, College Station, TX, and Lionel Levine, University of California at Berkeley, Berkeley, CA. Consider n unlabeled particles moving each at its own constant velocity along the real line. An observer is promised some number P of snapshots of the particles' positions, to be taken at uniformly spaced intervals of time. When particles coincide, the snapshot will show how many are at a given point.

(a) Show that if P = n + 1 then the observer can determine the velocities of each of the particles.

 (\mathbf{b}^*) As a function of n, what is the minimum value of P that will suffice to ensure that the observer can determine all n velocities?